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(*
                                CS51 Lab 8
                                Functors
                                Part 1
*)
```

(\* Objective:

This lab provides practice in the use of functors.

This part of the lab has been adapted from the functors chapter of Real World OCaml <<http://dev.realworldocaml.org/functors.html>>. \*)

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(*=====
Functors - Part 1.
```

For the first part of this lab, you will explore a realistic and useful application of functors -- a library to support interval computation.

Intervals come up in many different contexts. As a concrete example, calendars need to associate events with time intervals (3-4pm or 11:30am-3:30pm). Intervals can be empty (like the interval starting at 4pm and ending at the previous 3pm; it contains no time at all). We might want to know if a value is contained within an interval. (For example, 4pm is not contained within 11:30am-3:30pm, but is contained within 2-5pm.) We may want to know the intersection of two intervals. (The intersection of 3-4pm and 11:30am-3:30pm is 3-3:30pm.)

Importantly, intervals can be defined over different data types. For instance you may want to use intervals over floating point values or, as in the example above, intervals of times. But regardless of the type the intervals are over, you'll want some common basic operations: constructing an interval, checking if an interval is empty, checking if a point is contained within an interval, and intersecting two intervals. (Of course, in an actual interval library, you'd want several other operations as well, but this will be enough to get us started.)

Let's examine how we can build a *generic* interval library using functors.

An interval is defined by its endpoints. In order to operate on intervals, we need to be able to manipulate the endpoints as well, in particular by comparing two endpoints for how they are ordered. Thus, to define intervals over a certain kind of endpoints, we'll need the type of the endpoints and a comparison function.

The 'ORDERED\_TYPE' signature from the textbook (Section 12.3) will serve us nicely here. It uses the OCaml convention for comparison functions used by the 'Stdlib.compare' function:

```
compare x y < 0      (* x < y *)
compare x y = 0      (* x = y *)
compare x y > 0      (* x > y *)
*)
```

```
module type ORDERED_TYPE =
  sig
    type t
    val compare : t -> t -> int
  end ;;
```

```
(*.....
Exercise 1A: Complete the following functor for making interval modules.
```

We represent an interval with a variant type, which is either `'Empty'` or `'Interval (x, y)'`, where `'x'` and `'y'` are the bounds of the interval, and are themselves contained within the interval. The representation has an invariant that `'x'` is always less than or equal to `'y'` (where the notion of "less than or equal" is given by the `'compare'` function provided by the `'ORDERED_TYPE'` that the intervals are built from).

The functor definition starts out as

```
module MakeInterval (Endpoint : ORDERED_TYPE) =
  struct
    ...
  end
```

Here, the argument to the `'MakeInterval'` functor is a module, given the name `'Endpoint'` and constrained to satisfy the `'ORDERED_TYPE'` module signature. Thus, we know that `'Endpoint'` will provide both a type (`'Endpoint.t'`) and a comparison function over that type (`'Endpoint.compare'`). We can and will use those in defining the module being defined by the functor.

Now, complete the functor definition below.

.....\*)

```
module MakeInterval (Endpoint : ORDERED_TYPE) =
  struct
    type interval =
      | Interval of Endpoint.t * Endpoint.t
      | Empty

    (* create low high -- Returns a new interval covering 'low' to
       'high' inclusive. If 'low' is greater than 'high', then the
       interval is empty. *)
    let create (low : Endpoint.t) (high : Endpoint.t) : interval =
      failwith "create not implemented"

    (* is_empty intvl -- Returns true if and only if 'intvl' is
       empty *)
    let is_empty (intvl : interval) : bool =
      failwith "is_empty not implemented"

    (* contains intvl x -- Returns true if and only if the value 'x'
       is contained within 'intvl' *)
    let contains (intvl : interval) (x : Endpoint.t) : bool =
      failwith "contains not implemented"

    (* intersect intvl1 intvl2 -- Returns the intersection of 'intvl1'
       and 'intvl2' *)
    let intersect (intvl1 : interval) (intvl2 : interval) : interval =
      failwith "intersect not implemented"
  end ;;

  (*.....*)
  Exercise 1B: Using the completed functor above, instantiate an
  *integer* interval module.
  .....*)
```

```
module IntInterval =
  struct end ;; (* <-- replace this line with an appropriate module
                 definition using the 'MakeInterval' functor *)

  (*.....*)
  Exercise 1C: Using your newly created integer interval module, create
```

two non-empty intervals named `intvl1` and `intvl2` that have some overlap, and calculate their intersection as `intvl1\_intersect\_intvl2`.  
.....\*)

```
let intvl1 = failwith "not implemented" ;;
let intvl2 = failwith "not implemented" ;;
let intvl1_intersect_intvl2 = failwith "not implemented" ;;
```

(\* There's currently a problem with the `MakeInterval` functor. It's not abstract enough. Notably we are working with an invariant that a valid non-empty interval has an upper bound that is greater than or equal to its lower bound. However, this is only enforced by the `create` function, and as it turns out, we can actually bypass the `create` function due to our lack of an abstraction barrier.

This expression returns `true`, as expected.

```
IntInterval.is_empty (IntInterval.create 4 3) ;;
```

This, however, returns `false`. Yikes.

```
IntInterval.is_empty (IntInterval.Interval (4, 3)) ;;
```

\*\*Make sure you understand why this is a problem. If you don't see the issue, call over a staff member to discuss.\*\*

To make our functor more abstract, we need to restrict the output of `MakeInterval` to an interface that prevents users from directly creating interval implementations themselves without using the `create` function.

.....  
Exercise 2A: Complete the following interface for an interval module. Note in particular that we should add a new type `endpoint` to give us a way of abstractly referring to the type for the endpoints of an interval.  
.....\*)

```
module type INTERVAL =
  sig
    type interval
    type endpoint
    (* ... complete the interface here ... *)
  end ;;
```

(\*.....  
Exercise 2B: Augment the `MakeSafeInterval` functor using the code you wrote for `MakeInterval` as a starting point, such that it returns a module restricted to the `INTERVAL` signature. (Much of the implementation can be copied from `MakeInterval` above.) \*\*Don't forget to specify the module type.\*\*  
.....\*)

```
module MakeSafeInterval (Endpoint : ORDERED_TYPE) =
  struct
    (* ... complete the module implementation here ... *)
  end ;;
```

(\* We have successfully made our returned module abstract, but believe it or not, it is now too abstract. In fact, we have not exposed the type of endpoints to the user, meaning we cannot even create intervals now. The abstraction barrier is too strong. To demonstrate the problem ...

.....

Exercise 2C: Create an 'IntSafeInterval' module using the new 'MakeSafeInterval' functor.  
.....\*)

```
module IntSafeInterval =
  struct end ;; (* <-- replace this line with an appropriate module
                 definition using the 'MakeSafeInterval' functor *)
```

(\* Now, try evaluating the following expression in the REPL:

```
IntSafeInterval.create 2 3 ;;
```

A type error will appear:

```
Error: This expression has type int but an expression was expected of type
IntInterval.endpoint
```

To make the interface slightly less abstract, we can make use of a sharing constraint, which informs the compiler that a given type \*within\* the implementation is equal to some other type from \*outside\* the implementation. In this case, we want to inform the compiler the type of our endpoint is an 'int', and more generally that the type of our endpoint is 'Endpoint.t', where 'Endpoint' was the 'ORDERED\_TYPE' module that is the argument of the functor. We can do so with the following syntax:

```
<Module_type> with type <type> = <type'>
```

For instance, we can create int interval and float interval interfaces that reveal the type of endpoints as follows: \*)

```
module type INT_INTERVAL =
  INTERVAL with type endpoint = int ;;

module type FLOAT_INTERVAL =
  INTERVAL with type endpoint = float ;;
```

(\* Modules that satisfy these interfaces will allow users to actually construct intervals of the desired types.

While sharing constraints solve the abstraction issue discussed earlier, they now present a new problem. They will result in code duplication in implementation. The solution to this is to use sharing constraints in the MakeInterval functor, exposing that the type of an endpoint is equal to Endpoint.t. The functor can then be used to create interval modules of various types without duplicating code. That's what we'll do next. \*)

(\*.....\*)  
Exercise 3A: Define a new functor 'MakeBestInterval'. It should take an ORDERED\_TYPE module for the endpoints of the intervals, and return a module satisfying INTERVAL \*with appropriate sharing constraints to allow the creation of generic interval modules\*.

If you do this correctly, your code for 'MakeBestInterval' should be almost identical to your code for 'MakeSafeInterval' with the exception of any needed sharing constraints.  
.....\*)

(\* ... place your implementation of the MakeBestInterval functor here ... \*)

(\* We now have a fully functioning functor that can create interval modules of whatever type we want, with the appropriate abstraction level.

.....  
Exercise 3B: Use the 'MakeBestInterval' functor to create a new int interval module called 'IntBestInterval', and test that it works as expected.

You may for instance want to try the problematic lines from Exercise 1C.

The following expression should still return 'true', as expected:

```
IntBestInterval.is_empty (IntBestInterval.create 4 3) ;;
```

and this expression should no longer return 'false'. What does it return instead?

```
IntBestInterval.is_empty (IntBestInterval.Interval (4, 3)) ;;
```

```
.....*)
```

```
module IntBestInterval = struct end ;;
```